|  |  | tment of $f$ matics $\qquad$ | INDIAN SCHOOL AL WADI AL KABIR <br> Class IX, Mathematics <br> Worksheet-Triangles |  |  |  |  |  |
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| Q. No. | Questions of 1 Mark each. |  |  |  |  |  |  |  |
| 1. | Which of the following is not a criterion for congruence of triangles? |  |  |  |  |  |  |  |
|  | (A) | SAS | (B) | ASA | (C) | SSA | (D) | SSS |
| 2. | If $\mathrm{AB}=\mathrm{QR}, \mathrm{BC}=\mathrm{PR}$ and $\mathrm{CA}=\mathrm{PQ}$, then |  |  |  |  |  |  |  |
|  | (A) | $\triangle A B C \cong \triangle \mathrm{PQR}$ | (B) | $\triangle \mathrm{CBA} \cong \triangle \mathrm{PRQ}$ | (C) | $\triangle B A C \cong \triangle R P Q$ | (D) | $\triangle \mathrm{PQR} \cong \triangle \mathrm{BAC}$ |
| 3. | In triangles ABC and $\mathrm{PQR}, \mathrm{AB}=\mathrm{AC}, \angle \mathrm{C}=\angle \mathrm{P}$ and $\angle \mathrm{B}=\angle \mathrm{Q}$. The two triangles are: |  |  |  |  |  |  |  |
|  | (A) | Isosceles but not congruent | (B) | Isosceles and congruent | (C) | Congruent <br> but not isosceles | (D) | Neither congruent nor isosceles. |
| 4. | Observe the given triangles and choose the right answer. |  |  |  |  |  |  |  |
|  | (A) | $\triangle \mathrm{ABC} \cong \triangle \mathrm{QPR}$ | (B) | $\triangle \mathrm{ABC} \cong \triangle \mathrm{PQR}$ | (C) | $\triangle A B C \cong \triangle P R Q$ | (D) | $\triangle \mathrm{BAC} \cong \triangle \mathrm{RPQ}$ |
| 5. | It is given that $\triangle \mathrm{ABC} \cong \triangle \mathrm{FDE}$ and $\mathrm{AB}=5 \mathrm{~cm}, \angle \mathrm{~B}=40^{\circ}$ and $\angle \mathrm{A}=80^{\circ}$. Then which of the following is true? |  |  |  |  |  |  |  |
|  | (A) | $\begin{aligned} & \mathrm{DF}=5 \mathrm{~cm}, \\ & \angle \mathrm{~B}=60^{\circ} \end{aligned}$ | (B) | $\begin{aligned} & \mathrm{DE}=5 \mathrm{~cm}, \\ & \angle \mathrm{E}=60^{\circ} \end{aligned}$ | (C) | $\begin{aligned} & \mathrm{DF}=5 \mathrm{~cm}, \\ & \angle \mathrm{E}=60^{\circ} \end{aligned}$ | (D) | $\begin{aligned} & \mathrm{DE}=5 \mathrm{~cm}, \\ & \angle \mathrm{D}=40^{\circ} \end{aligned}$ |


| 6. | In figure, if $\mathrm{AB}=\mathrm{DC}, \angle \mathrm{ABD}=\angle \mathrm{CDB}$, which congruence <br> rule would you apply to prove $\triangle \mathrm{ABD} \cong \triangle \mathrm{CDB}$ ? |
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| 7. | In the given figure, prove that $\triangle \mathrm{ABD} \cong \triangle \mathrm{BAC}$ ? |
| Civen $\triangle \mathrm{OAP} \cong \triangle \mathrm{OBP}$ in the figure below. Prove |  |
| criteria by which the triangles are congruent. |  |
| In the given figure, $\angle \mathrm{ACB}=\angle \mathrm{BDA}, \angle \mathrm{ABD}=\angle \mathrm{BAC}$. Prove that $\triangle \mathrm{AOB}$ is |  |


| 10. | In the figure, if $\mathrm{AF}=\mathrm{CD}, \angle \mathrm{AFE}=\angle \mathrm{CDE}$, <br> Prove that $\mathrm{EF}=\mathrm{ED}$. |
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| 11. | Prove that the angle opposite to equal sides of a triangle are equal |
| 12. | ABC is an isosceles triangle with $\mathrm{AB}=\mathrm{AC} . \mathrm{P}$ and Q are <br> points on AB and AC respectively such that $\mathrm{AP}=\mathrm{AQ}$, <br> Prove that $\angle \mathrm{ACP}=\angle \mathrm{ABQ}$, and $\mathrm{CP}=\mathrm{BQ}$. |
| 13. | In the figure below, ABCD is a square and P is the mid- <br> point of AD . BP and CP are joined. Prove that <br> $\angle \mathrm{PCB}=\angle \mathrm{PBC}$. |


| 14. | In figure, $\mathrm{AB}=\mathrm{EF}, \mathrm{BC}=\mathrm{ED}, \mathrm{AB} \perp \mathrm{BD}, \mathrm{EF} \perp \mathrm{EC}, \mathrm{Prove}$ <br> that $\triangle \mathrm{ABD} \cong \triangle \mathrm{FEC}$. |
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| 15. | In the given figure, if $\mathrm{AB} \\| \mathrm{DC}$ and P is the mid-point of BD, <br> Prove that P is also the mid-point of AC. |
| 16. | In the figure, $\mathrm{OA}=\mathrm{OB}, \mathrm{OC}=\mathrm{OD}$ and $\angle \mathrm{AOB}=\angle \mathrm{COD}$. Prove that <br> $\mathrm{AC}=\mathrm{BD}$. |
| 17. | In figure, $\triangle \mathrm{ABC} \cong \triangle \mathrm{ABD}$ are such that $\mathrm{AD}=\mathrm{BC}, \angle 1=\angle 2$ and <br> $\angle 3=\angle 4 . ~ P r o v e ~ t h a t ~$ <br> $\mathrm{BD}=\mathrm{AC}$. |


| 18. | In fig. $\mathrm{AD}=\mathrm{CD}$ and $\mathrm{AB}=\mathrm{CB}$. State three pairs of equal parts in $\triangle \mathrm{ABD} \cong \triangle \mathrm{CBD}$. Is $\triangle \mathrm{ABD} \cong \triangle \mathrm{CBD}$ ? Why <br> or why not? Does BD bisect $\angle \mathrm{ABC}$ ? Give reasons. <br> 19. <br> CASE STUDY: <br> A triangular based agricultural field $A B C$ is divided <br> by the farmer in four parts. In two parts of his field he <br> wants to grow sugarcane and other two parts he wants <br> to grow wheat. He wants to grow wheat on the field <br> division exactly which are exactly same in shape and <br> size, the same he wants to do sugarcane. <br> If $\triangle \mathrm{ABC}$ and $\triangle \mathrm{DBC}$ are two isosceles triangles on the same base BC and vertices A and D are on the same <br> side BC . AD is extended to intersect BC at P . <br> With reference to the figure given, answer the following questions. <br> i)Prove that $\triangle \mathrm{ABD} \cong \triangle \mathrm{ACD}$. <br> ii) Prove that $\triangle \mathrm{APB} \cong \triangle \mathrm{APC}$. |
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| 20. | $A B$ is a line segment. $P$ and $Q$ are points on opposite sides of $A B$ such that each of them is equidistant from the points $A$ and $B$. Show that the line PQ is the perpendicular bisector of AB . |  |  |  |  |  |  |  |
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|  | Answers |  |  |  |  |  |  |  |
| $\begin{aligned} & \mathscr{0} \\ & 0 \\ & 0 \\ & 0 \\ & \vdots \end{aligned}$ | 1 | C | 2 | B | 3 | A | 4 | QA |
|  | 5 | C | 6 | SAS | 7 | $\begin{gathered} \mathrm{AD}=\mathrm{BC}, \\ \mathrm{AB}=\mathrm{BA} \\ \angle \mathrm{D}=\angle \mathrm{C}=90^{\circ} \\ \text { By RHS } \end{gathered}$ | 8 | $\begin{gathered} O A=O B, \\ \angle 1=\angle 2, O P=O P \\ \text { BY SAS } \end{gathered}$ |
|  | 9 | $\begin{gathered} \angle \mathrm{C}=\angle \mathrm{D}, \\ \mathrm{AB}=\mathrm{AB} \\ \angle \mathrm{ABD}=\angle \mathrm{BAC} \\ \mathrm{By} \mathrm{AAS} \end{gathered}$ | 10 | $\begin{gathered} \mathrm{AF}=\mathrm{CD}, \\ \angle \mathrm{AFE}=\angle \mathrm{CDE} \\ \angle \mathrm{E}=\angle \mathrm{E} \\ \text { By AAS } \end{gathered}$ | 11 | $\begin{gathered} \angle 1=\angle 2, \\ \mathrm{AD}=\mathrm{AD}, \\ \mathrm{AB}=\mathrm{AC} \\ \mathrm{By} \text { SAS } \end{gathered}$ | 12 | $\begin{gathered} \mathrm{AB}=\mathrm{AC}, \mathrm{AP}=\mathrm{AQ}, \\ \angle \mathrm{~A}=\angle \mathrm{A} \\ \mathrm{By} \text { SAS } \end{gathered}$ |
|  | 13 | $\begin{gathered} \mathrm{AP}=\mathrm{DP}, \mathrm{AB}=\mathrm{DC} \\ \angle \mathrm{~A}=\angle \mathrm{D}=90^{\circ} \\ \text { By } \mathrm{SAS} \end{gathered}$ | 14 | $\begin{gathered} \mathrm{AB}=\mathrm{EF} \\ \angle \mathrm{~B}=\angle \mathrm{E}=90^{\circ} \\ \mathrm{BC}=\mathrm{ED} \\ \mathrm{BC}+\mathrm{CD}=\mathrm{ED}+\mathrm{CD} \\ \mathrm{BD}=\mathrm{EC}, \mathrm{By} \text { SAS } \end{gathered}$ | 15 | $\begin{aligned} & \mathrm{BP}=\mathrm{DP}, \\ & \angle 1=\angle 2, \\ & \angle 3=\angle 4 \\ & \text { By AAS } \end{aligned}$ | 16 | $\begin{gathered} \mathrm{OA}=\mathrm{OB}, \\ \mathrm{OC}=\mathrm{OD}, \\ \angle \mathrm{AOB}=\angle \mathrm{COD} \\ \angle \mathrm{AOC}=\angle \mathrm{BOD} \\ \mathrm{By} \text { SAS } \end{gathered}$ |
|  | 17 | By SAS | 18 | By SSS | 19 | By SAS | 20 | To be proved by using SSS and SAS |

